Online Sabotaged Shortest Path



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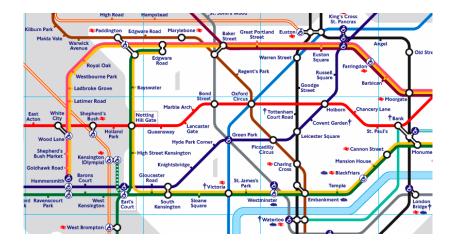
Dmitry Adamskiy

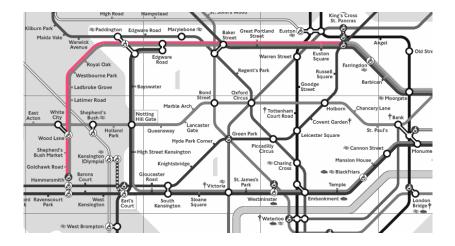


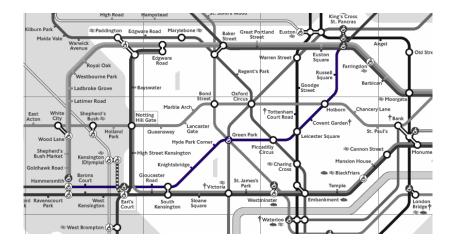


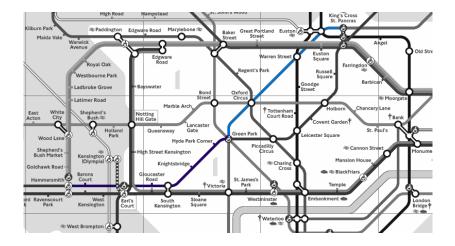


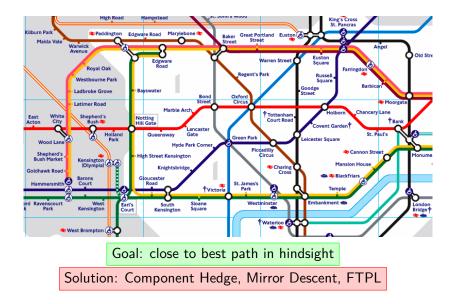




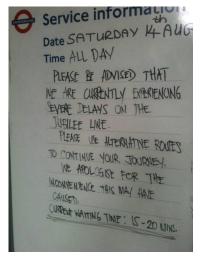








Adversarial losses...



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"Good service on all other London Undergound lines"

Adversarial losses...

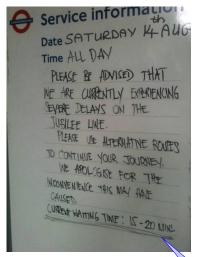


... and some paths are blocked



"Good service on all other London Undergound lines"

Adversarial losses...



... and some paths are blocked



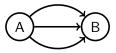


"Good service on all other London Undergound lines"

Previous work: policy regret

Compete with policy for choosing alternatives to blocked paths...

In fully adversarial setting it is computationally hard already for experts [Kanade and Steinke, 2014]:



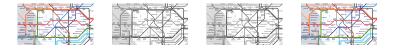
 If sabotages are stochastic and losses are decoupled from them, then efficient algorithms exist [Neu and Valko, 2014]

Proposed notion of regret

We seek a natural notion of regret that avoids the hardness.

Get back to basics and compete with the path only on the rounds when it is awake.

$$\begin{array}{l} \mathsf{Regret}(\mathsf{Path}) = \sum_{\substack{\mathsf{rounds when path} \\ \mathsf{is awake}}} \left(\mathsf{loss}(\mathsf{Learner}) - \mathsf{loss}(\mathsf{Path})\right) \end{array}$$



Time

The Open Problem

Is there an efficient algorithm for our regret?

- Less expressive than policies
- Historically the first notion of sleeping
- Efficient algorithm for expert setting
- Naive, grossly inefficient algorithm gets

 $\mathsf{Regret}(\mathsf{Path}) \leq \mathsf{Diameter}\sqrt{T \log |\mathsf{Paths}|}$